



# E-BOOK

## INEQUALITIES

## CONCEPT

# SuperGrads Study Material

Part of the most Comprehensive Classroom Training, Prep Content & Test Series across the Nation.

## QUANTITATIVE ABILITY



## TIPS FOR INEQUALITY

### Concept 01

- The topic Inequalities is one of the few sections in the quantitative part which can throw up tricky questions. The questions are often asked in conjunction with other sections like ratio and proportion, progressions etc.
- The theory involved in Inequalities is very limited and students should be comfortable with the basics involving addition, multiplication and changing of signs of the inequalities.
- The scope for making an error is high in this section as a minor mistake in calculation (like forgetting the sign) can lead to a completely different answer.

### Concept 02

- The modulus of  $x$ ,  $|x|$  equals the maximum of  $x$  and  $-x$   
 $-|x| \leq x \leq |x|$
- For any two real numbers 'a' and 'b',  
 $|a| + |b| \geq |a + b|$   
 $|a| - |b| \leq |a - b|$   
 $|a \cdot b| = |a| |b|$
- If  $|x| \leq k$  then the value of  $x$  lies between  $-k$  and  $k$ , or  $-k \leq x \leq k$
- If  $|x| \geq k$  then  $x \geq k$  or  $x \leq -k$

### Concept 03

- For any three real numbers  $X$ ,  $Y$  and  $Z$ ; if  $X > Y$  then  $X+Z > Y+Z$
- If  $X > Y$  and
  1.  $Z$  is positive, then  $XZ > YZ$
  2.  $Z$  is negative, then  $XZ < YZ$
  3. If  $X$  and  $Y$  are of the same sign,  $\frac{1}{X} < \frac{1}{Y}$
  4. If  $X$  and  $Y$  are of different signs,  $\frac{1}{X} > \frac{1}{Y}$

### Concept 04

- For any positive real number,  $x + \frac{1}{x} \geq 2$
- For any real number  $x > 1$ ,  
 $2 < \left[1 + \frac{1}{x}\right]^x < 2.8$

As  $x$  increases, the function tends to an irrational number called 'e' which is approximately equal to 2.718

### Concept 05

- If  $ax^2 + bx + c < 0$  then  $(x - m)(x - n) < 0$ , and if  $n > m$ , then  $m < x < n$
- If  $ax^2 + bx + c > 0$  then  $(x - m)(x - n) > 0$  and if  $m < n$ , then  $x < m$  and  $x > n$
- If  $ax^2 + bx + c > 0$  but  $m = n$ , then the value of  $x$  exists for all values, except  $x$  is equal to  $m$ , i.e.,  $x < m$  and  $x > m$  but  $x \neq m$